

1 **A goal-programming approach to allocate Freight Analysis Framework mode flow data**

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**ABSTRACT**

Several methods have been proposed to disaggregate Freight Analysis Framework (FAF) commodity flows to zonal structures of greater geographical detail. This disaggregation is usually performed on the basis of explanatory variables related to the supply and demand of goods. In this paper a complementary procedure is presented to determine the mode splits of disaggregated FAF flows. A goal-programming approach is proposed to allocate FAF mode flow data on the basis of mode-related variables. The formulated goal-programming problem minimizes the deviation between the mode flow decision variables and target mode flow values, subject to given FAF mode flow information. The use of mode split models is proposed to define the problem's target values. In a sample application of the procedure a method to estimate aggregate mode split models with FAF data is discussed. These mode split models could be used by transportation organizations that do not have access to freight mode choice models to define the goal-programming problem's target mode flow values. Additionally, an optimization problem is formulated to account for FAF mode flow data in the disaggregation of total commodity flows. Lastly, validation procedures for FAF disaggregation and mode allocation results are discussed, and an example of a validation approach is presented.

**Keywords:** Freight Analysis Framework, disaggregation procedures, goal-programming problems, aggregate mode split models

## 1 INTRODUCTION

2  
3 Commodity-based freight transportation models attempt to capture the relationship between the supply and  
4 demand of goods by different economic sectors and the resulting generation of freight movements. Given  
5 its focus on the driving forces behind the demand for freight transportation, this modeling approach permits  
6 the analysis of sophisticated scenarios and policy questions of interest to metropolitan and state  
7 transportation organizations. Unfortunately, many transportation agencies do not have access to the  
8 commodity flow data necessary to develop these types of models, either because the data have not been  
9 collected, its purchase from third parties is prohibitively expensive, or the available data do not exist at the  
10 necessary level of geographic detail. In response to this data availability problem, methods have been  
11 developed to derive the commodity flows of interest from public data sources. The FHWA's Freight  
12 Analysis Framework regional database (FAF) is one of such public data sources available to transportation  
13 analysts in the US (1).

14 The latest version of the Freight Analysis Framework, FAF<sup>3</sup>, contains commodity flow data – in  
15 term of annual tons, ton-miles, and dollar value – on 43 different types of commodity groups. The FAF<sup>3</sup>  
16 database includes commodity flow information for 123 domestic and eight international origin-destination  
17 (OD) regions, the latter being used to account for the export and import of commodities. The database also  
18 provides commodity flow information by mode of transportation categories, namely, truck, rail, water, air  
19 (including air-truck), multiple modes and mail, pipeline, other and unknown, and the “no domestic mode”  
20 category used for import flows (1). This comprehensive database has the potential of addressing some of  
21 the data gaps facing many transportation agencies, and thus several methods have been developed to  
22 disaggregate FAF commodity flows to zonal structures with greater geographical detail.

23 The methodology presented in this paper can be regarded as a second-stage procedure following  
24 the distribution of FAF flows to sub-FAF zonal levels. As will be discussed in the next section, the  
25 disaggregation of FAF flows is generally performed by computing or estimating expansion factors that are  
26 functions of variables related to the supply and demand of goods. In this paper it is proposed that the  
27 disaggregated commodity flows can then be split into mode-specific flows by using variables related to  
28 freight mode choice. A goal programming-based procedure is discussed to determine the mode splits of  
29 disaggregated FAF commodity flows. The objective of the goal-programming problem is to minimize the  
30 difference between sub-FAF mode flows and associated target mode flow values subject to sets of  
31 constraints that ensure consistency with the FAF mode flow data. Mode split models and analyst  
32 assumptions can be used to define target flows for each mode.

33 The next section reviews previous efforts to disaggregate the FAF database. The third section  
34 presents the general outline of the procedure to determine the disaggregated flows mode splits. This is  
35 followed by a case study application of the proposed methodology in which a method to estimate aggregate  
36 mode split models using FAF<sup>3</sup> data is discussed. The fourth section integrates previous disaggregates  
37 approaches with the goal-programming model. The last section discusses possible future research and  
38 applications of the proposed models.

## 39 LITERATURE REVIEW

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42 One of FAF's data products comprise sets of truck flows assigned to selected highway links. These  
43 estimated truck flows are the result of a procedure that disaggregates the FAF level OD flows to  
44 corresponding freight activity centers at the county or sub-county level. These activity centers include major  
45 manufacturing plants, truck-rail intermodal terminals, seaports, airports, and other truck-generating urban  
46 clusters. For each center a measure related to the production or consumption of freight is computed, and its  
47 division by the corresponding FAF total activity constitutes the share of the total flow allocated to the  
48 center. In FAF's second version (FAF<sup>2</sup>), the freight activity measure for domestic flows was a function of  
49 the number of industrial establishments associated with each center (as reported in the 2005 County  
50 Business Patterns) and related annual vehicle-miles travelled (VMT, obtained from the 2002 Highway  
51 Performance Monitoring System). A similar procedure was followed to disaggregate international truck

1 freight flows, but the disaggregation was performed considering truck flow data at international  
2 crossings (2).

3 Viswanathan *et al.* (3) note that employing VMT in the computation of disaggregation factors has  
4 several drawbacks, including the fact that truck VMT measures capture non-freight related truck traffic  
5 (e.g., utility and service truck VMT), truck traffic that is merely passing by the activity center but not  
6 originating from or arriving at the center, or both. Therefore, Viswanathan *et al.* proposed creating  
7 commodity-specific disaggregation factors using the freight flows estimates of freight production and  
8 attraction models, akin to generation models in four-step commodity-based freight models. The  
9 commodity-specific production and attraction models were specified as functions of different types of  
10 employment and, for selected commodities, population. In contrast to the previous methodology, this  
11 methodology considers total OD flows, rather than the truck OD flows. Viswanathan *et al.* estimated the  
12 models using FAF domestic data as the dependent variable. The equations were then applied at the  
13 county and FAF zonal levels to estimate freight production and attraction. These estimates were used to  
14 compute proportional production and attraction weighting factors that map the total FAF OD flow to  
15 their corresponding sub-FAF OD zones. Opie *et al.* (4) also applied proportional weighting methods to  
16 disaggregate FAF data to county level zones, but in their study the production and attraction factors were  
17 computed by directly dividing the county level proxy variable (e.g., employment, population, VMT) by the  
18 related FAF level proxy variable. In contrast, in the methodology proposed by Ruan and Lin (5) the  
19 disaggregation factors that map FAF OD flows to sub-FAF OD flows were jointly estimated with the  
20 freight production and attraction equations.

21 As would be expected, a common theme in the reviewed studies is that the zones with higher values  
22 of the identified proxy production or consumption variables are allocated greater portions of the FAF  
23 OD flows. In the studies by Viswanathan *et al.* (3) and Ruan and Lin (5) this relationship was formalized  
24 with the estimation of freight production and consumption equations. In the next section, a procedure that  
25 splits the disaggregated FAF commodity flows into mode flows based on the given FAF mode data is  
26 presented. And, analogous to the use of freight production and attraction models used in the previously  
27 discussed disaggregation procedures, the proposed methodology allocates the modal flows according to  
28 mode split model estimates.

### 30 **MODE FLOW ALLOCATION PROCEDURE**

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32 Consider the FAF level commodity flow  $F_{Ijc}$  for origin  $I$ , destination  $J$ , and commodity group  $c$ , and its  
33 disaggregated flows  $f_{ijc}$ , where  $i \in I$  and  $j \in J$ . The objective is to determine reasonable mode flow splits  
34 for each  $f_{ijc}$  that are in agreement with the FAF modal information. Let  $m_{ijck}$  represent the flow by mode  
35  $k$  between zones  $i$  and  $j$ , and  $M_{Ijck}$  represent the given FAF level mode flow between zones  $I$  and  $J$ . For  
36 an OD, a mode flow allocation is in agreement with the FAF level information if it satisfies the following  
37 constraints:

$$38 \quad \sum_i \sum_j \alpha_{ijck} m_{ijck} = M_{Ijck} \quad \forall k \quad (1)$$

$$\sum_k m_{ijck} = f_{ijc} \quad \forall i, j \quad (2)$$

$$m_{ijck} \geq 0 \quad \forall i, j, k \quad (3)$$

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40 The first constraint ensures that, for each mode  $k$ , the sum of all sub-FAF  $m_{ijck}$  flows equals the  
41 parent  $M_{Ijck}$  flow.  $\alpha_{ijck}$  is a coefficient that indicates if there is access to mode  $k$  between zones  $i$  to  $j$ , an  
42 important consideration for the rail, water and pipeline modes. The second constraint guarantees that the  
43 proposed mode flows  $m_{ijck}$  add to the total commodity flow  $f_{ijc}$ . Given this set of constraints, a reasonable  
44 allocation of the FAF mode flows can be determined by solving the following goal-programming problem:

$$\text{Minimize } X = \sum_i \sum_j \sum_k |m_{ijck} - \hat{m}_{ijck}| \quad (4)$$

subject to constraints (1) – (3)

The values  $\hat{m}_{ijck}$  are target (or goal) mode split values. Therefore, the solution to the goal programming problem are the mode flows  $m_{ijck}$  that result in the least absolute deviation from the target values. Defining the target mode splits for each OD  $ij$  is a subjective task that depends, in part, on the analyst's judgment. One approach to objectively define the target  $\hat{m}_{ijck}$  values is to multiply the  $f_{ijc}$  flows by mode shares estimated via a mode split model. However, given that it is unlikely for a mode split model to consider all FAF modes (e.g., consider the other and unknown mode category), complementary assumptions might be required for ODs with modes out of the mode split model scope.

Note that the objective function can be linearized by introducing variables that measure the positive ( $PD_{ijck}$ ) or negative ( $ND_{ijck}$ ) deviations between each  $m_{ijck}$  and  $\hat{m}_{ijck}$ . The problem is then reformulated as:

$$\text{Minimize } Y = \sum_i \sum_j \sum_k (PD_{ijck} + ND_{ijck}) \quad (5)$$

subject to constraints (1) – (3) and

$$PD_{ijck} - ND_{ijck} = m_{ijck} - \hat{m}_{ijck} \quad \forall i, j, k \quad (6)$$

$$PD_{ijck} \geq 0, ND_{ijck} \geq 0 \quad \forall i, j, k \quad (7)$$

The presented objective function could easily be substituted by other formulations, such as a least squares objective function. However, considering that the goal-programming model must be solved for each FAF OD being disaggregated and for each commodity group of interest, a linear objective function is presented since it is one of the least computationally demanding formulations of the problem. Besides the selection of objective function, it should also be noted that another possible modification is formulating the problem in terms of mode shares (instead of mode flows).

An alternative methodology to the one presented in this section is to perform the FAF flow disaggregation for each mode's commodity flow OD matrix separately, instead of disaggregating the total commodity flow OD matrix and then allocating the flows to mode groups (the approach assumed in this study). The latter approach can be considered as conceptually more appealing as it extends the argument that data disaggregation procedures should be based on variables related to what is being disaggregated. In the case of disaggregating procedures for commodity flows, the variables of interest are those related to the demand and supply of goods. Analogously, variables associated with freight mode choice, such as modal service attributes and decision-maker characteristics, should be used for the mode allocation of disaggregated flows. Moreover, although disaggregating each mode's commodity flow OD matrix separately has the benefit of circumventing the need for a commodity flow mode allocation procedure, the mode-specific disaggregation factors generated in this approach may undercut the rationale for using production and consumption variables to compute FAF disaggregation factors. This is because these mode-specific factors would generally rely on the same zonal demand and supply variables (e.g., population, employment, farmland acres). Since each mode transports a different amount of goods, mode-specific disaggregation factors could imply that for each mode the explanatory variables result in different rates of consumption and production, which might not be reasonable. This observation is particularly meaningful when production and attraction models are estimated to develop disaggregation factors (e.g., see 3, 4). As an example, consider an analyst interested in modeling the zonal production and attraction (or consumption) of agricultural shipments using farmland acreage as a production variable and population as an attraction

1 variable. A zone's population has a single demand level for agricultural products, not distinct demand levels  
 2 by mode, as the consumption decisions of each person do not account for which modes were used to  
 3 transport the products. Similarly, the farmland production levels at each zone do not vary by mode, but, in  
 4 part, as a function of the aggregate demand. Therefore, if the analyst is interested in computing  
 5 disaggregation factors that reflect the supply and demand dynamics associated with agricultural product  
 6 markets, he/she should use total production and consumption of commodity flows instead of introducing  
 7 data segmentations that, although convenient, may mask the causal connections between the flows and the  
 8 selected explanatory variables.

9 The next section presents an application of the proposed procedure. In addition, a method to  
 10 estimate mode split models using FAF data is discussed, which might be useful for transportation agencies  
 11 that have not developed or do not have access to freight mode split model.

## 12 **SAMPLE APPLICATION OF THE PROPOSED PROCEDURE**

13 The domestic commodity flow of manufactured metal products between the Los Angeles FAF zone and the  
 14 Houston FAF zone was selected for the application of the allocation procedure. The definition of the  
 15 manufactured metal products commodity group is taken from Ranaiefar *et al.* (6). This commodity group  
 16 is composed of FAF<sup>3</sup>'s base metal, articles-based metals, and machinery groups. The FAF<sup>3</sup> database for  
 17 domestic movements reports 324.6 ktons flow of manufactured metal products from the Los Angeles FAF  
 18 zone to the Houston FAF zone, of which 73.4 percent was transported by truck, 18.4 percent was transported  
 19 by rail, 7.5 percent was transported by multiple modes, and 0.7 percent was transported by air-truck. The  
 20 disaggregated zonal structure for California's FAF zones presented by Ranaiefar *et al.* was used in this  
 21 study. Figure 1 shows the disaggregated Los Angeles zone; the Houston FAF zone is not disaggregated as  
 22 it is regarded as an external zone. The rail stations shown in Figure 1 represent those stations that are known  
 23 to handle manufactured metal products flows according to the 2007 Surface Transportation Board Carload  
 24 Waybill Sample (CW) (7). Additionally, Figure 1 presents the truck-rail intermodal facilities in the area.

### 25 **Disaggregating commodity flows**

26 The methodology proposed by Viswanathan *et al.* (3) was implemented to disaggregate the 324.6 ktons  
 27 flow. This methodology was previously used by Cambridge Systematics to disaggregate California's FAF<sup>2</sup>  
 28 domestic flows (8). The freight production model estimated by Ranaiefar *et al.* (6) with FAF<sup>3</sup> data was used  
 29 for the disaggregation. This model is a function of the number of establishments in the fabricated metal  
 30 product manufacturing industry (industry 332 in the North American Industry Classification System) and  
 31 the manufacturing sector's gross domestic product. Given that the destination zone is not disaggregated,  
 32 the equation used to obtain the sub-FAF level flows using the proportional weighting method is:

$$33 \quad f_{ijc} = F_{Ijc} \times \frac{p_{ic}}{p_{Ic}} \quad (11)$$

34 For the OD under consideration,  $F_{Ijc}$  is the FAF level flow of 324.6 ktons.  $p_{Ic}$  and  $p_{ic}$  are the total  
 35 generation of manufactured metal products by the Los Angeles zone and the related sub-FAF origins,  
 36 respectively, as predicted by the production models. Table 1 presents the computed  $f_{ijc}$  flows for the  
 37 example under consideration.

### 38 **Allocating mode flows**

39 As mentioned in the previous section, the targets of the goal-programming problem can be determined using  
 40 mode flow estimates from mode split models. However, the same data availability challenges encountered  
 41 with commodity flow data are encountered with freight mode choice data. Therefore, the estimation of an  
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1 aggregate mode split model using FAF<sup>3</sup> data is discussed in this subsection. This procedure might be useful  
 2 for transportation agencies that do not have access to a suitable mode choice model. Alternatively, agencies  
 3 in this situation could also consider borrowing the parameters from another organization's freight mode  
 4 split model, and attempt to update the parameters based on available mode data (e.g., mode shares from  
 5 FAF).

6 The multivariate fractional regression (MFR) model (or fractional split model) was selected to  
 7 estimate an aggregate mode split model for the manufactured metal products commodity group. The MFR  
 8 model structure has been used in transportation studies to examine commodity flow distribution (9), time-  
 9 use allocation (10), highways' VMT mix (11), and to estimate binomial freight mode split models (12).  
 10 Model parameters in the MFR model are estimated using a quasi-likelihood estimation approach. The MFR  
 11 model is used to estimate the expected values for fractional dependent variables. It is especially useful when  
 12 a non-negligible number of observed fractions take boundary values of zero or one.

13 In the current application the MFR model was estimated using California-related mode shares as  
 14 the dependent variables. These mode shares were computed using FAF mode flows that had an origin or  
 15 destination in California. Similar to the approach taken by Viswanathan *et al.* (3) and Ranaiefar *et al.* (6),  
 16 the model was estimated using FAF level data, but applied at the sub-FAF geographical scale. Only three  
 17 modes were included in the model: truck, rail, and multiple modes and mail. The multiple modes and mail  
 18 category was incorporated in the model because of the importance of the truck-rail mode in mode shift  
 19 analyses. Unfortunately, as its name indicates, in addition to truck-rail the multiple modes and mail category  
 20 includes modes such as truck-water, rail-water, and, most importantly, mail and parcel. Therefore,  
 21 assumptions are required to remove the non-truck-rail component of FAF's multiple modes and category.  
 22 For simplicity, in this study the 2007 Commodity Flow Survey (CFS) (13) was used to obtain commodity  
 23 and OD specific factors to subtract the mail and parcel flows from FAF's multiple modes and mail category,  
 24 and the remaining flow was modeled as if it was truck-rail flow. The CFS information is presented for state  
 25 level ODs, so the factors are state OD specific. For example, the CFS data for the manufactured metal  
 26 products flows between California and Texas shows that mail and parcel represents 2 percent of the total  
 27 flow. Given the stated assumptions, this implies that 6.6 ktons of the Los Angeles-Houston flow is  
 28 transported by the mail and parcel mode, while the remaining 17.6 ktons in the multiple modes category is  
 29 modeled on the basis of truck-rail modal attributes.

30 A multinomial logit formulation was assumed for the MFR model as this functional form is often  
 31 used in aggregate freight mode split modeling (14). Therefore, the target mode flows  $\hat{m}_{ijck}$  were computed  
 32 as follows:  
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$$\hat{m}_{ijck} = f_{ijc} \times \frac{e^{\gamma_{ijck}}}{\sum_n e^{\gamma_{ijcn}}} \quad (12)$$

34  $\gamma_{ijck}$  was specified as:  
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$$\gamma_{ijck} = \beta_{0k} + \beta_{cost} \log(cost_{ijck}) + \beta_{time} \log(time_{ijck}) \quad (13)$$

37  $\beta_{0k}$  is the mode  $k$  specific constant,  $\beta_{cost}$  is the coefficient of the cost attribute, and  $\beta_{time}$  is the coefficient  
 38 of the transit time attribute. This specification attempts to capture the effects of cost and transit time on  
 39 freight mode shares, a standard practice in aggregate mode split models. Demo-economic variables (12),  
 40 measures of commodity values and the magnitude of the mode flows themselves are examples of other  
 41 explanatory variables that could be considered in the specification of  $\gamma_{ijck}$ .  
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43 The cost variable ( $cost_{ijck}$ ) was computed by multiplying mode  $k$ 's shortest path distance between  
 44 OD  $ij$  by that mode's shipping freight rate (\$/ton-mile). The equation for the rail and truck-rail modes was  
 45 estimated using the California-related carload data in the CW. This equation is a function of distance, a  
 46 dummy variable for intermodal shipments, location dummies (i.e., dummies that indicate from which state  
 47 the shipment originated or arrived), and an interaction term between distance and the intermodal dummy.

1 The truck freight rate equation was estimated using data from a commercial freight rates database (15), and  
 2 is a function of distance, average fuel price in the region of origin (16), and, again, location dummies. An  
 3 additional freight rates model was estimated for short-haul truck movements using as explanatory variables  
 4 fuel, dummies for origin zones, and lag rate variables of the second order. This short-haul truck rate equation  
 5 was used to quantify the drayage cost associated with truck-rail cost; the drayage cost was added to the  
 6 truck-rail rail-haul cost. The three freight rate equations were estimated using stepwise linear regression.  
 7 Additional assumptions related to truck-rail terminal costs were made based on information presented by  
 8 Resor and Blaze (17). The rate functions are not included in this paper due to space limitations, but are  
 9 available upon request. Distanced-based functions were used to compute transit times for the truck, rail,  
 10 and truck-rail modes. These functions are also available upon request.

11 Table 2 presents the estimated parameters for the aggregate mode split mode. Truck-rail is selected  
 12 as the reference so its alternative specific constant is set to zero. Table 1 shows the mode split model target  
 13 values for the truck, rail and truck-rail modes, as well as the uniformly distributed target flows for the  
 14 remaining modes. The targets for the remaining mode flows (the air and the subtracted mail and parcel  
 15 mode flows) are the total  $f_{ijc}$  flows multiplied by their corresponding aggregate mode share. Table 1 also  
 16 presents two solutions to the optimization problem: the solution for the least absolute deviations objective  
 17 function ( $L_1$ ) and the solution for the least squares objective function ( $L_2$ ). By design, both solutions add to  
 18 the FAF<sup>3</sup> mode flows, so the analyst must judge which objective function result is more reasonable, given  
 19 available data and constraints.

20 Ortuzar and Willumsen note that aggregate mode split model results “may turn out to be very  
 21 approximate” (14). Not surprisingly, the same could be observed with models estimated using the FAF<sup>3</sup>  
 22 mode flow data, particularly given the size of FAF zones and the related levels of data aggregation. In the  
 23 presented example, the last row in Table 1 shows that the target mode flows underestimate the FAF rail  
 24 flow for the selected OD pair while overestimating the truck and truck-rail flows. In general, a reason for  
 25 the relative inaccuracy of aggregate mode split models is that zonal level average cost and time measures  
 26 fail to capture the influence of several important mode choice determinants, such as perceptions of mode  
 27 travel time reliability, mode accessibility, and shipment characteristics. The development of additional  
 28 proxy variables to account for these factors is a possible way to improve model accuracy.

## 30 ENSURING CONSISTENCY BETWEEN DISAGGREGATED FLOWS AND FAF MODE DATA

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 32 For some ODs the existence of feasible solutions to the goal-programming problems will depend on whether  
 33 the FAF mode information was taken into account when disaggregating the total commodity flows. If the  
 34 flows are disaggregated solely on the basis of the information provided by surrogate freight generation  
 35 variables, the resulting flows may conflict with the FAF mode data. As an example, consider the FAF<sup>3</sup>  
 36 animal feed commodity flow from California’s “remainder zone” to Hawaii’s “remainder zone”. Activities  
 37 associated with the production of animal feed (e.g., the harvest of hay) occur throughout all counties of  
 38 California’s “remainder zone”, so a disaggregation based on this commodity’s freight production variables  
 39 would generate flows originating from all the counties in this zone. However, the FAF modal information  
 40 for this OD indicates that its animal feed flow is transported exclusively by the water mode (which does  
 41 not include truck-water flows). Thus, the goal-programming problem for this OD would be infeasible as  
 42 not all counties in California’s “remainder zone” have seaports, and consequently constraint set (1) could  
 43 not be satisfied. Similar incongruities could arise for other ODs with rail, water or pipeline flows, as the  
 44 facilities required to access these modes are not as ubiquitous as roadways. Therefore, a procedure is  
 45 required to ensure that the total commodity flow disaggregation results,  $f_{ijc}$ , do not conflict with the FAF  
 46 mode data. Define  $R_{IJ}$  as the set of all modes with non-zero flow from  $I$  to  $J$  that have mode availability  
 47 restrictions (i.e., modes that are not available in all  $ij$  pairs), and  $r$  as a mode in that set. Furthermore, let  
 48  $\alpha_{ijcR}$  refer to an indicator variable that assumes the value of one when a mode in  $R$  is available in OD  $ij$ .  
 49 Then, a set of disaggregated flows that are consistent with the FAF mode data can be determined by solving  
 50 the following problem:



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$$\text{Minimize } Z = \sum_i \sum_j |f_{ijc} - \hat{f}_{ijc}| \quad (14)$$

subject to

$$\sum_i \sum_j \alpha_{ijck} f_{ijc} \geq M_{IJck} \quad \forall k \quad (15)$$

$$\sum_i \sum_j \alpha_{ijcR} f_{ijc} \geq \sum_r M_{IJcr} \quad (16)$$

$$f_{ijc} \geq 0 \quad \forall i, j \quad (17)$$

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The target values  $\hat{f}_{ijc}$  can be obtained via one of the disaggregation procedures reviewed. The  $\alpha_{ijck}$  indicators in constraint set (15) have the same interpretation as in constraint set (1). Constraints (15) ensure that, for each mode  $k$ , the sum of the allocated flows to zones with access to mode  $k$  is greater than or equal to the corresponding FAF mode flow. However, since it is possible for modes in  $R$  to be present in the same zones, the constraints (15) might allow for solutions in which the combined flow for all  $r$  modes cannot be satisfied. Thus constraint (16) ensures that the combined flow of zones with modes in set  $R_{IJ}$  is greater than or equal to the related FAF mode flow. If the  $\hat{f}_{ijc}$  targets satisfy constraints (15) and (16) no adjustment occurs (i.e.,  $f_{ijc}$  equals  $\hat{f}_{ijc}$  for all  $ij$  pairs). This is the case of the example presented in section 4. Conversely, in situations like the one presented in the animal feed example the modal information would completely override the disaggregation suggested by the production and attraction variables. Note that objective function (14) can be linearized, and it could also be substituted by formulations such as least squares deviations. Figure 2 presents a schematic of the integrated procedure suggested by the two optimization problems presented.

## POSSIBLE VALIDATION PROCEDURES FOR DISAGGREGATION AND MODE FLOW ALLOCATION RESULTS

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Testing the validity of disaggregated commodity flows and the related mode allocations at the sub-FAF level is primarily hindered by the same problem that motivates the use of FAF disaggregation and mode allocation procedures, namely, the dearth of commodity flow data at county and sub-county levels. FAF disaggregation studies (e.g., 3, 4) have attempted to validate their model results with county level data from Transearch, a proprietary database (21). These comparisons have shown non-trivial discrepancies between FAF and Transearch, in part because of definitional and conceptual differences between the two databases (3). An alternative approach to Transearch-based validations is to compare modeled traffic assignments resulting from the estimated sub-FAF mode flows with observed transportation network data. Ideally these network data would be available for all the modes and commodity types, but in reality it is unlikely that a transportation agency has this level of information. Nevertheless, typically transportation agencies do collect truck count data at major roadways, and these data could allow for the creation of cordon, screenline, or cutline counts that can be used for a partial validation of the commodity flow disaggregation and truck allocation results without requiring significant data collection efforts. This validation approach requires of multiple assumptions, such as percentage of empty trucks, percentage of service trucks, tonnage-to-truck conversion factors, and seasonality factors. Available literature, including FAF<sup>3</sup> documentation (22), provides reference values that can be used by transportation agencies to make informed assumptions on unknown factors. Note that, unless the transportation agency can identify the types of commodities being moved by the observed trucks, the truck count validation approach would have to be performed on the basis of aggregated truck counts, not commodity-specific truck counts.

1 In this study neither Transearch nor extensive truck count data were available to perform validation  
2 tests. However, for illustrative purposes Southern California truck assignments flows, estimated in part by  
3 procedures presented in this study, were compared to cutline counts (i.e., corridor level counts) (Figure 3).  
4 The comparisons between cutline and modeled counts have been suggested as an aggregate level validation  
5 and reasonableness check for travel models (23). The cutlines used in this study were created with 2007  
6 truck count data from eight weight-in-motion (WIM) stations located at major highways in the region.  
7 FAF<sup>3</sup>-based county and sub-county flows for all commodities were borrowed from preliminary results of  
8 the California Statewide Freight Forecasting Model's (CSFFM) commodity generation and distribution  
9 modules (6). These disaggregated commodity flows were allocated to truck, rail, truck-rail, and "remainder  
10 mode" categories using the least absolute deviation goal-programming model. The goal-programming  
11 problem targets were defined by FAF-based MFR mode split models and complementary assumptions  
12 similar to the ones presented in the sample application section. Factors based on the 2002 Vehicle Inventory  
13 and Use Survey were used to convert truck tonnage flows to truck vehicle flows, and to add empty trucks  
14 (24). Additionally, truck vehicle flows were converted from annual to daily flows utilizing the CSFFM  
15 truck seasonality model. The truck segments of truck-rail movements were associated to transshipment  
16 facilities using the CSFFM transshipment model. Finally, the truck flows were assigned to a model of  
17 California's truck road network using a stochastic truck assignment model. The WIM stations data labeled  
18 each truck with the corresponding vehicle classification. Consequently, in this study the comparisons  
19 between the modeled and observed daily truck volumes could focus on the truck classes more likely to be  
20 carrying commodities in California (FHWA vehicle classes 8, 9, and 10). Table 3 reports the WIM and  
21 mode counts for each cutline, as well as the percent errors. Significant errors were observed for cutlines 2a,  
22 4a, and 4b. There could be multiple reasons for these errors, including model prediction errors (e.g.,  
23 commodity flow distribution, mode allocation), incorrect assumptions (e.g., percent of empty trucks), and  
24 even data problems in FAF<sup>3</sup>. Given the limited extend of the cutlines (which is the result of limited  
25 availability of reliable truck counts), in this study it was not possible to identify with confidence what are  
26 the reasons for the discrepancies between the WIM and model counts. But this example demonstrates a  
27 relatively standard approach that can be used by transportation agencies to check if their FAF commodity  
28 flow disaggregation and mode allocation results are consistent with network observations.  
29

## 30 CLOSING REMARKS

31  
32 A goal-programming approach was presented for the mode allocation of disaggregated FAF commodity  
33 flows. The proposed method is intended as a second-step procedure following the distribution of FAF flows  
34 to sub-FAF zonal levels. A framework was suggested to connect previous total commodity flow  
35 disaggregation procedures with the optimization problems proposed in this paper. Note that the structure of  
36 the integrated procedure presented in Figure 2 is similar to the structure of the four-step commodity-based  
37 freight forecasting model, where commodity flow generation and mode split models are usually the first  
38 and third steps, respectively. This integrated framework could be expanded by introducing optimization  
39 problems to recalibrate the commodity flow disaggregation or mode allocation outputs based on traffic  
40 assignment results obtained from the mode flow allocations (the fourth step in the four-step model) and  
41 observed transportation network data. The formulation of these optimization problems could be the subject  
42 of future research. Additional research is also needed on the development of the FAF-based mode split  
43 models. For example, clustering procedures could be utilized to segment the commodity flow data (e.g.,  
44 based on magnitude of the flow), and then separate mode split models could be estimated with each data  
45 group. Also, the utility of more complex model functional forms (e.g., nested logit) should be explored.

46 For agencies that do not have access to freight mode choice models, a method was proposed to  
47 estimate aggregate mode split models using FAF data. In this paper these models were presented as a way  
48 to define target values for the goal-programming models. However, the mode split models could also be  
49 used by these agencies to perform aggregate level policy analysis, as the mode split model coefficients  
50 reflect to some degree the sensitivity of mode shares to changes in modal attributes, such as transit costs. A  
51 possible modeling approach is to develop incremental logit models by borrowing the parameters of the

1 estimated mode split models and using sub-FAF mode shares (or even the FAF mode shares) as the base  
2 shares. However, caution should be taken in the estimation, interpretation, and use of FAF-based aggregate  
3 mode split models since segments of the FAF data itself are the result of several intermediate models,  
4 especially for the CFS out-of-scope commodity flows (1, 13).

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**TABLE 1 Results for Disaggregation and Mode Flow Allocation Procedures**

Zones	$f_{ijc}$	Target Mode Flows				$L_1$ Solution				$L_2$ Solution			
		T	R	TR	RM	T	R	TR	RM	T	R	TR	RM
603700	2.4	2.1	0.0	0.2	0.1	2.1	0.0	0.2	0.1	1.8	0.0	0.1	0.5
603701	1.9	1.7	0.0	0.2	0.1	1.7	0.0	0.2	0.1	1.4	0.0	0.1	0.5
<b>603702</b>	17.0	12.8	2.2	1.5	0.5	12.8	3.7	0.0	0.5	11.8	4.5	0.6	0.1
603703	2.7	2.4	0.0	0.3	0.1	2.4	0.0	0.3	0.1	2.0	0.0	0.2	0.5
603704	22.8	19.9	0.0	2.3	0.6	19.9	0.0	2.3	0.6	19.6	0.0	2.2	1.0
<b>603705</b>	30.0	22.8	3.8	2.6	0.8	5.1	24.2	0.0	0.8	21.7	6.1	1.7	0.5
<b>603706</b>	16.2	12.3	2.1	1.4	0.4	12.3	3.5	0.0	0.4	11.2	4.4	0.5	0.1
<b>603707</b>	28.6	21.7	3.6	2.5	0.8	21.7	6.1	0.0	0.8	20.6	5.9	1.6	0.4
<b>603708</b>	13.2	10.0	1.7	1.1	0.4	10.0	2.8	0.0	0.4	8.9	4.0	0.3	0.0
603709	0.7	0.6	0.0	0.1	0.0	0.6	0.0	0.1	0.0	0.3	0.0	0.0	0.4
<b>603710</b>	8.9	6.7	1.1	0.8	0.2	6.7	1.9	0.0	0.2	5.6	3.3	0.0	0.0
<b>603711</b>	33.6	25.6	4.2	2.9	0.9	25.6	4.5	2.7	0.9	24.5	6.5	2.0	0.6
605900	29.3	25.6	0.0	2.9	0.8	25.6	0.0	2.9	0.8	25.3	0.0	2.8	1.2
605901	3.7	3.2	0.0	0.4	0.1	3.2	0.0	0.4	0.1	2.9	0.0	0.3	0.5
<b>605902</b>	29.1	22.1	3.7	2.5	0.8	22.1	3.7	2.5	0.8	21.0	6.0	1.7	0.4
<b>605903</b>	15.6	11.9	2.0	1.3	0.4	11.9	3.3	0.0	0.4	10.8	4.3	0.5	0.1
606500	8.7	7.6	0.0	0.9	0.2	7.6	0.0	0.9	0.2	7.3	0.0	0.7	0.7
606501	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
606502	1.7	1.5	0.0	0.2	0.0	1.5	0.0	0.2	0.0	1.2	0.0	0.1	0.5
<b>606503</b>	13.0	9.9	1.6	1.1	0.4	9.9	1.6	1.1	0.4	8.8	3.9	0.2	0.0
<b>607100</b>	18.2	13.9	2.3	1.6	0.5	13.9	2.3	1.6	0.5	12.8	4.6	0.7	0.1
<b>607101</b>	2.3	1.8	0.3	0.2	0.1	1.8	0.5	0.0	0.1	0.2	2.1	0.0	0.0
<b>607102</b>	13.9	10.6	1.7	1.2	0.4	10.6	1.7	1.2	0.4	9.5	4.0	0.3	0.0
611100	11.1	9.6	0.0	1.1	0.3	9.6	0.0	1.1	0.3	9.3	0.0	1.0	0.7
Total	324.6	256.1	30.3	29.3	8.8	238.4	59.8	17.6	8.8	238.4	59.8	17.6	8.8

Notes: T=Truck, R=Rail, TR=Truck-Rail, RM=Remaining Modes. Zones with rail accessibility have bold identifications.  
All flows in kton units.

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**TABLE 2 Estimated Parameters for the MFR Model**

<b>Name</b>	<b>Value</b>	<b>Robust t-stat</b>
$\beta_{0,truck}$	1.980	6.60
$\beta_{0,rail}$	0.517	0.79
$\beta_{0,truck-rail}$	0	-
$\beta_{cost}$	-0.413	-1.85
$\beta_{time}$	-0.947	-3.52

Sample size : 253  
 Null log-likelihood : -277.9  
 Final log-likelihood : -125.3  
 $\bar{\rho}^2$  : 0.535

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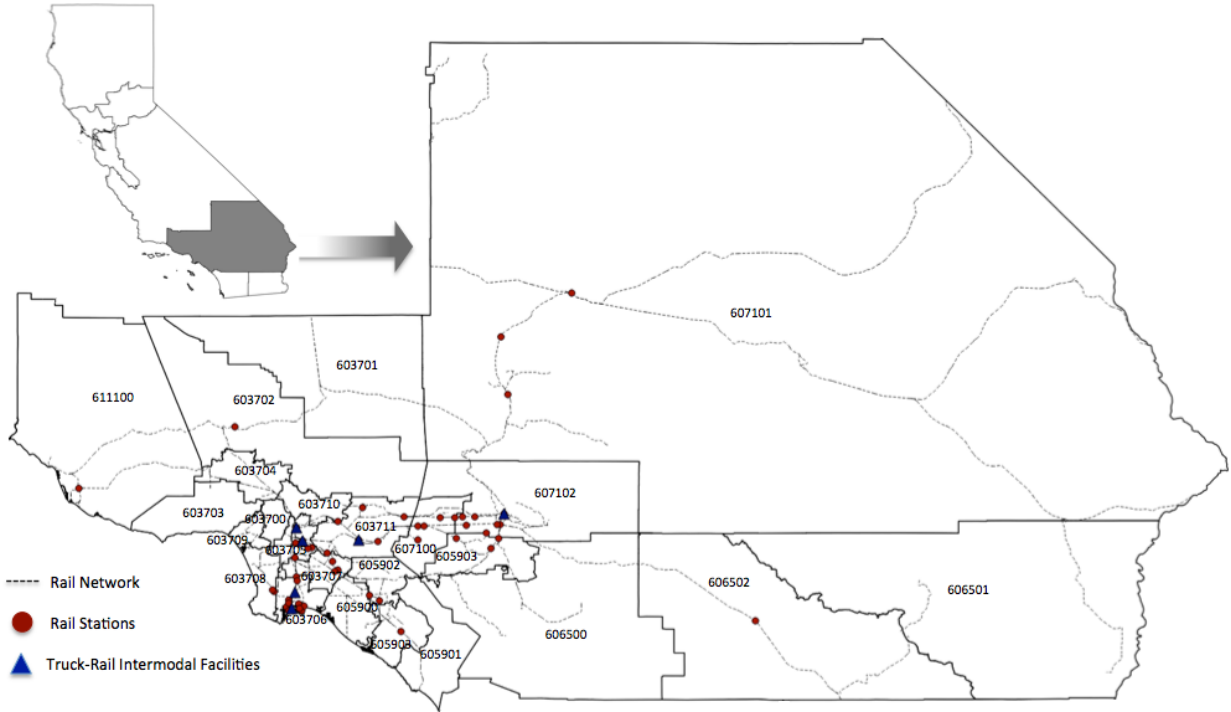
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**TABLE 3 Comparison between modeled and observed truck counts**

<b>Cutlines</b>	<b>Cutline Volume Direction Description</b>	<b>WIM Counts</b>	<b>Model Counts</b>	<b>Percent Error</b>
1	Leaving through east of Los Angeles County	10574	10966	3.7%
2a	Leaving San Bernardino County toward Arizona	5949	3841	-35%
2b	Entering San Bernardino County from Arizona	6190	6862	10%
3	Leaving Orange County toward east direction	9878	9094	-7%
4a	Leaving Riverside County toward east and south directions	7348	10657	45%
4b	Entering Riverside County from east and south directions	5900	8172	38%

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**FIGURE 1** Disaggregated zonal structure for the Los Angeles FAF<sup>3</sup> zone.

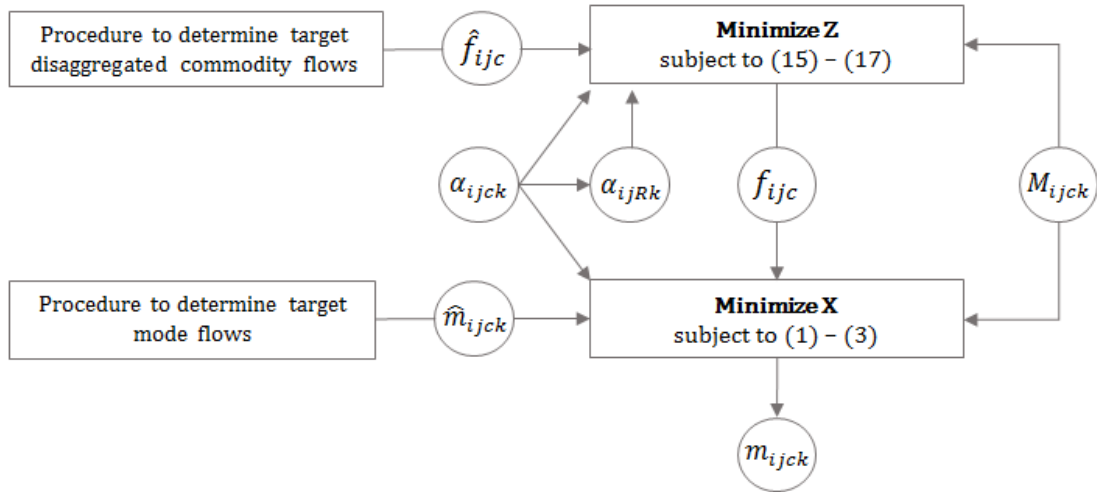
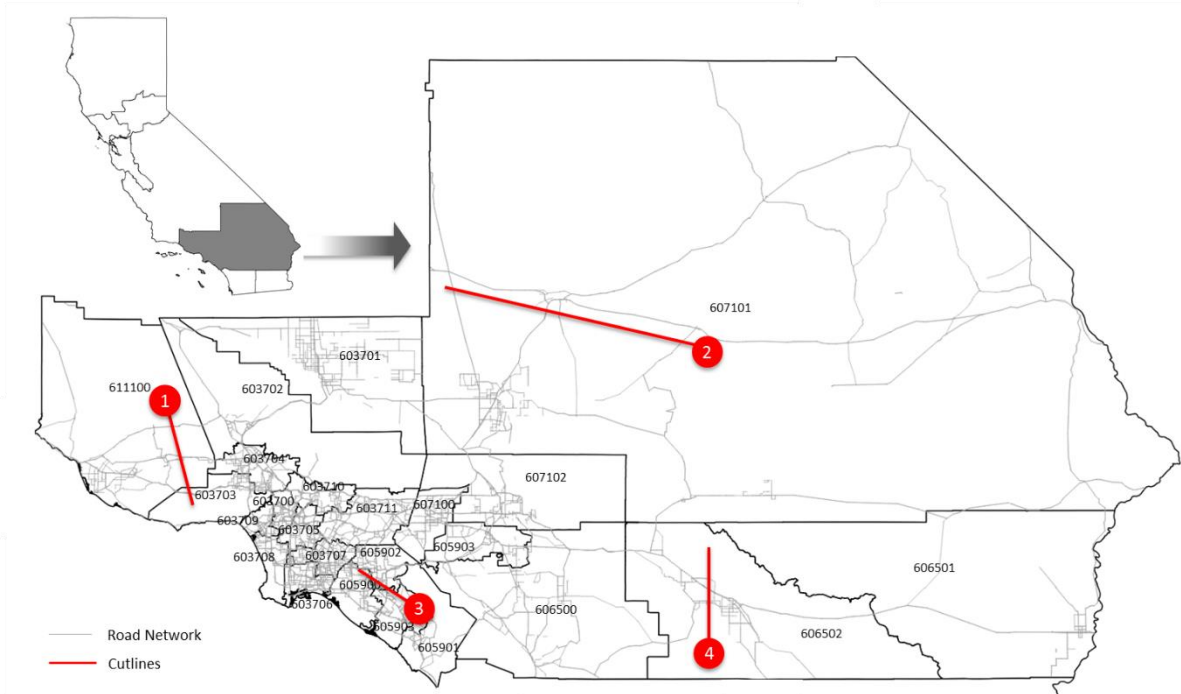


FIGURE 2 Framework to disaggregate commodity flows and allocate mode flows for a FAF OD.

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2 **FIGURE 3** Approximate location of the corridor cutlines.